

# On Accurate Packet Loss Estimation for Networks without Traffic Models

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## Introduction

- It is important to accurately model network traffic when we evaluate Quality of Service (QoS) of networks through simulations.
  - It is difficult to select an appropriate traffic model and tune its parameters.
  - Even if the accurate traffic modeling is achieved, it is also difficult to accurately estimate QoS regarding rare events.

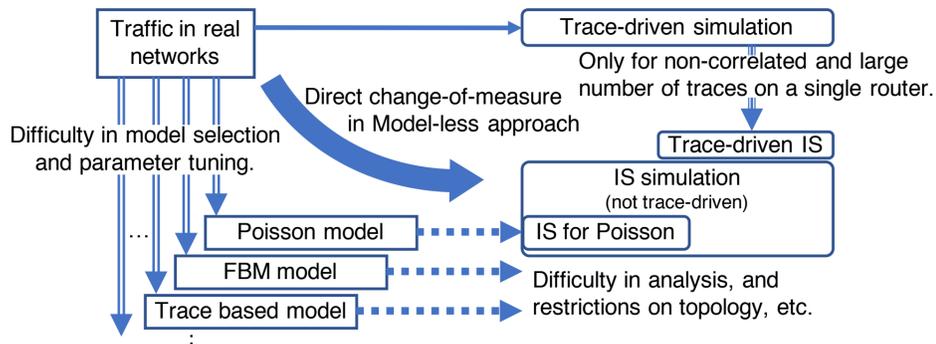


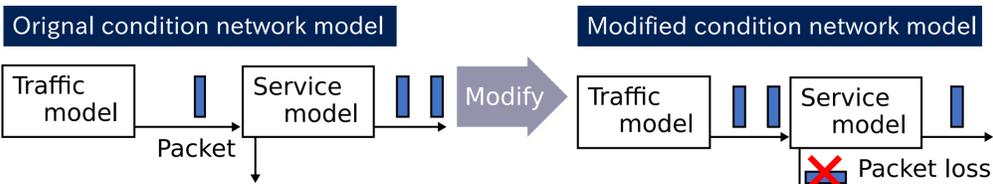
Figure 1: The model-less approach and the conventional simulations.

- Importance Sampling (IS) for accurate estimations of rare events [2]
  - The events occur more frequently in IS simulation.
  - The estimator is obtained by the change-of-measure.
  - The applicable traffic models, topology etc. are extremely limited.
- Trace-driven IS without traffic models [3]
  - It cannot be applied for single flow traffic.
  - It is not applicable for traffic with correlated flows.

## Goal of our study

- We propose a model-less approach to accurately estimate a packet loss rate through a simulation without directly modeling traffic, including real network traffic.

## Model Based IS



Estimator of IS

$$\hat{l}_{IS} = \frac{1}{\tilde{c}} \sum_{j=1}^{\tilde{c}} \left\{ \mathbf{1}_{\{j \in \phi\}} \frac{p(\omega)}{\tilde{p}(\omega)} \right\}$$

Change-of-measure

$$\tilde{l} = \frac{1}{\tilde{c}} \sum_{j=1}^{\tilde{c}} \mathbf{1}_{\{j \in \phi\}}$$

$\tilde{c}$ : The number of packets,  $\phi$ : The set of lost packets,  $\omega$ : The queue length process,  
 $p(\omega)$ : Probability density of an event  $\omega$  in the original condition,  
 $\tilde{p}(\omega)$ : Probability density of an event  $\omega$  in the modified condition.

Figure 2: Outline of model base IS

- When IS estimates a loss rate on a single router into which a single flow streams, the change-of-measure is performed based on probability density of a path  $\omega$  of the queue length process [2].
- The change-of-measure  $p(\omega)/\tilde{p}(\omega)$  is analytically derived from a traffic model in model-based IS.

## Model-less Approach

- Our goal is to accurately estimate a packet loss rate through a simulation in a real network without assuming any traffic model.

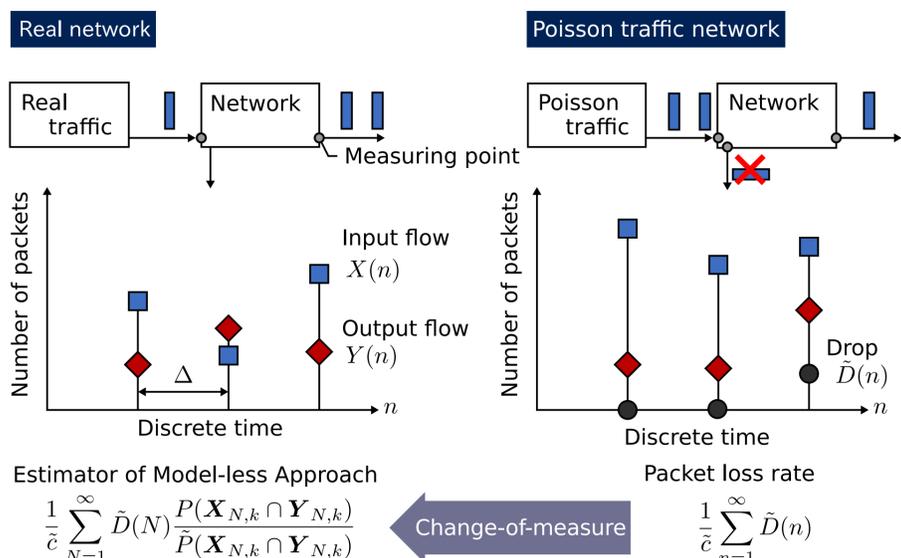


Figure 3: Outline of model-less approach

- The model-less approach follows the procedure below.
  - A simulation with Poisson traffic model is performed.
  - Input traffic, output traffic and loss processes are discretized with  $\Delta$ .
  - Change-of-measure is based on frequency of discretized traffic pattern.
- Our estimator is

$$\hat{l} = \frac{1}{\tilde{c}} \sum_{N=1}^{\infty} \tilde{D}(N) \frac{P(\mathbf{X}_{N,k} \cap \mathbf{Y}_{N,k})}{\tilde{P}(\mathbf{X}_{N,k} \cap \mathbf{Y}_{N,k})}, \quad (1)$$

where

$\mathbf{X}_{N,k} = \{X(n)\}_{N-k < n \leq N}$ : Discretized input flow traffic in past  $k$  periods.  
 $\mathbf{Y}_{N,k} = \{Y(n)\}_{N-k < n \leq N}$ : Discretized output flow traffic in past  $k$  periods.  
 $\tilde{D}(n)$ : Discretized packet loss process.

- When we assume a single router and a single flow, in the limit as  $\Delta \rightarrow 0$  and  $k \rightarrow N$ , our estimator converges to that of model based IS.
- By expressing the estimator by input and output traffic instead of a queue length process, (1) is applicable for multiple flows on a network with complicated topology.

## Experiments

- As a first step in the development, we investigate the case when the packet loss rate of an MMPP/M/1/K system is estimated from an M/M/1/K simulation.
- The simulation time is 2000 [s], simulation sets is 30,  $\Delta = 0.025$  [s], and  $k = 2$ .
- In these systems, since the packet arrivals and a service time are independent.
- Therefore, the change-of-measure can be expressed as  $P(X_{1,N,k} \cap Y_{1,N,k})/\tilde{P}(X_{1,N,k} \cap Y_{1,N,k}) = P(X_{1,N,k})/\tilde{P}(X_{1,N,k})$ .

Table 1: Target network parameters

|   |           |
|---|-----------|
| Arrive Rate at State 1 [packet/s]       | 100       |
| Arrive Rate at State 2 [packet/s]       | 339       |
| Transition Rate of Each State [times/s] | 1.00      |
| Mean Service Time [s/packet]            | 0.001     |
| Queue Size $K$ [packet]                 | 10        |
| Packet Loss Rate [-]                    | $10^{-5}$ |

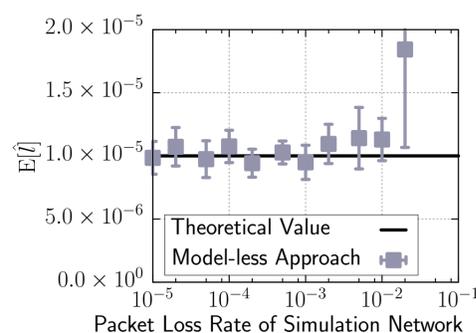


Figure 4: Result of mean

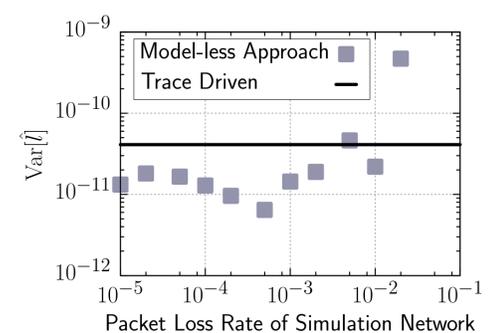


Figure 5: Result of variance

- According to the figures, we can find the region in which the model-less approach can estimate the packet loss rate of the original system.
- Additionally, we can confirm that the variances of the estimators are about 1/3 in the region, compared with the estimator by the trace-driven simulation.

## Conclusions and Future Directions

- We proposed the model-less approach to accurately estimate a packet loss rate through simulation with traffic trace without traffic models.
- We will verify the applicability of our approach to the various trace on various networks in our future works.

## References

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